

BALLARI INSTITUTE OF TECHNOLOGY & MANAGEMENT

(Autonomous Institute under Visvesvaraya Technological University, Belagavi)

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Course Code

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Third Semester B.E. Degree Examinations, March/April 2023

BASIC SIGNAL PROCESSING-I

Duration: 3 hrs.

Max. Marks: 100

Note: 1. Answer any FIVE full questions, choosing ONE full question from each module.
2. Missing data, if any, may be suitably assumed

<u>Q. No</u>	<u>Question</u>	<u>Marks</u>	<u>(RBT:CO:PI)</u>
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MODULE – 1

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| 1. | a. Define Signal and System. Explain the important elementary signals with suitable mathematical expressions and waveform. | 08 | (2:1: 1.3.1) |
| | b. Find the even and odd components of following signals. | 08 | (3:1: 2.1.3) |
| | i) $x(t) = 1 + t \cos(t) + t^2 \sin(t) + t^3 \sin(t) \cos(t)$ | | |
| | ii) $x(t) = \begin{cases} 1 & -1 \leq t \leq 1 \\ 2 & 1 \leq t \leq 2 \\ 0 & \text{otherwise} \end{cases}$ | 04 | (4:1: 5.1.1) |
| | c. Write the MATLAB script to plot sine signal $x(t)$, when $x(t) = 5 \sin\left(8\pi t + \frac{\pi}{3}\right)$ $0 \leq t \leq 2T$ where $T = \frac{2\pi}{\omega}$ fundamental period | | |
| | (OR) | | |
| 2. | a. Find whether the following signals are energy or power signals and find its energy or power | 08 | (3:1: 2.1.3) |
| | i) $x(n) = \cos(\pi n) - 3 \leq n \leq 3$ ii) $x(t) = 6 \cos(\pi t) + 3 \sin(4\pi t)$. | | |
| | b. For the following system, determine whether the system is (i) Linear (ii) Time-invariant (iii) Memory less and (iv) Causal. $y(t) = \cos(x(t))$ | 08 | (3:1: 2.1.3) |
| | c. Write the MATLAB script to plot $x(-2t - 4)$ when $x(t) = \sin(t)$. | 04 | (4:1: 5.1.1) |

MODULE – 2

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|----|--|----|---------------|
| 3. | a. Evaluate the discrete time convolution sum given and also plot the output $y(n) = \left(\frac{1}{2}\right)^n \cdot u(n-2) * u(n)$. | 08 | (3 :2: 2.1.3) |
| | b. State and prove commutative and associative property of convolution. | 08 | (2 :2: 1.3.1) |
| | c. Write the MATLAB script to find convolution of $y(n) = x(n) * h(n)$ when $x(n) = [1, 2, 3, 1]$ and $h(n) = [2, 1, -1, 3]$. | 04 | (4 :2: 5.1.1) |
| | (OR) | | |
| 4. | a. An LTI system is characterized by an impulse response, $h(n) = \left(\frac{3}{4}\right)^n u(n)$. Find the step response of the system. | 08 | (3:2: 2.1.3) |
| | b. Investigate causality and stability of the following System. | 08 | (3 :2: 2.1.3) |
| | i) $h(t) = e^{-2 t }$ ii) $h(n) = 2^n u(n-1)$ | | |
| | c. Write the MATLAB script to find impulse response of system $h(n)$ for difference equation $y(n) - \frac{4}{9}y(n-1) = x(n-1)$ | 04 | (4 :2: 5.1.1) |

MODULE – 3

5. a. State and prove the following properties of CTFT 08 (3:3:1.3.1)
i) Time Shift ii) Time differentiation
- b. Evaluate the Fourier transform for the following signals. Sketch the magnitude. i) $x(t) = e^{-3t}u(t-1)$ ii) $x(t) = e^{-|t|}$. 08 (3 :3: 2.1.3)
- c. Write the MATLAB script to find Fourier transform of $x(t) = t e^{-2t}u(t)$. 04 (4 :3: 5.1.1)

(OR)

6. a. Determine the continuous time signal corresponding to each Fourier transform. 08 (3 :3:2.1.3)
i) $X(\omega) = \frac{2 \sin [3(\omega-2\pi)]}{\omega-2\pi}$ ii) $X(\omega) = \cos (4\omega + \pi/3)$.
- b. State and prove the modulation property. 08 (2 :3: 1.3.1)
- c. Write the MATLAB script to perform Amplitude modulation. 04 (4 :3: 5.1.1)

MODULE – 4

7. a. Determine the DTFT of the following signal and draw its spectrum 10 (3 :3:2.1.3)
$$x(n) = \left(\frac{1}{2}\right)^n u(n-4).$$
- b. State and prove the following properties of DTFT. 10 (3 :3: 1.3.1)
i)Time Shifting ii) Parseval theorem

(OR)

8. a. Find the inverse DTFT of $x(e^{j\Omega}) = (3-0.25e^{-j\Omega})/(-0.1e^{-j2\Omega}+1)$ 10 (3 :3:2.1.3)
- b. Find the DTFT of $x(n)=a^{|n|}$ $|a|<1$, Also sketch magnitude and phase 10 (3 :3: 1.3.1)

MODULE – 5

9. a. Explain briefly the ROC and its important properties. 10 (2 :5: 1.3.1)
- b. Find the Z-transform of the following signals and indicate their ROC 10 (3 :3: 2.1.3)
i) $x(n)=-a^n u(-n-1)$ ii) $x(n)= (1/3)^n \sin(\pi n/4) u(n)$

(OR)

10. a. Find the inverse Z transform for the given $x(z) = \frac{4+2z^{-1}}{(4-z^{-1})(2-z^{-1})(1-z^{-1})}$ 10 (3 :3: 2.1.3)
For ROC i) $|z|>1$ ii) $|z|<0.25$ iii) $0.5<|z|<1$ 10 (3 :3: 2.1.3)
- b. A causal LTI system is described by $y(n)-\frac{3}{4}y(n-1) + \frac{1}{8}y(n-2) = x(n)$, where $x(n)$ and $y(n)$ are the input and output of the system respectively.
- i)Find the system function $H(z)$
- ii)Find the impulse response $h(n)$
- iii)Find the BIBO stability of the system

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