06

(1:1:1.2.1)

(3:1:1.2.1)

BALLARI INSTITUTE OF TECHNOLOGY & MANAGEMENT

(Autonomous Institute under Visvesvaraya Technological University, Belagavi)

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USN						Course Code 2)	2	M	A	\mathbf{T}	S	1	1

First Semester B.E. Degree Summer Semester Examinations, September/October 2025

MATHEMATICS-I FOR COMPUTER SCIENCE & ENGINEERING STREAM

Duration: 3 hrs Max. Marks: 100

- Note: 1. Answer any FIVE full questions, choosing ONE full question from each module.
 - 2. Missing data, if any, may be suitably assumed
 - 3. Use of Mathematics Formula Handbook is permitted.

Module-1

- 1. a. Find the rank of the following matrix by row echelon
 - form $A = \begin{bmatrix} 2 & 3 & -1 & -1 \\ 1 & -1 & -2 & -4 \\ 3 & 1 & 3 & -2 \\ 6 & 3 & 0 & 7 \end{bmatrix}$
 - **b.** Investigate the values of λ and μ such that the system of equations x+y+z=6; x+2y+3z=10, $x+2y+\lambda z=\mu$ may have (i) Unique solution
 - (ii) Infinite solution (iii) No solution.
 - **c.** Solve the following system of equations by Gauss elimination method 2x+y+4z=12, 4x+11y-z=33, 8x-3y+2z=20.

- 2. a. Solve the following system of equations by Gauss-Jordon elimination 06 (3:1:1.2.1) method 2x+3y-z=5; 4x+4y-3z=3; 2x-3y+2z=2.
 - **b.** Solve the following system of equations using Gauss Seidel method $20x + y 2z = 17; \ 3x + 20y z = -18; 2x + 3y + 20z = 25$
 - c. Find the dominant Eigen value and the corresponding Eigen vector of the 07 (3:1:1.2.1)

matrix
$$A = \begin{bmatrix} 2 & 0 & 1 \\ 0 & 2 & 0 \\ 1 & 0 & 2 \end{bmatrix}$$
 by Rayleigh's power method taking the initial

Eigen vector as $\begin{bmatrix} 1 & 1 & 1 \end{bmatrix}^T$.

Module-2

- 3. a. Prove that for the curve $r = f(\theta) \frac{1}{p^2} = u^2 + \left(\frac{du}{d\theta}\right)^2$ where $u = \frac{1}{r}$.
 - **b.** Find the angle between the pairs of curves $r = a(1 + \cos \theta)$ and 07 (3:2:1.2.1) $r = b(1 \cos \theta)$
 - c. Find the pedal equation of the curve $r^n = a^n \cos \theta$ (3:2:1.2.1)

 (OR)

4. **a.** Prove with usual notation:
$$\rho = \frac{(1+y_1^2)^{3/2}}{y_2}$$
 06 (2:2:1.2.1)

b. Find the radius of curvature of
$$a^2y = x^3 - a^3$$
 where the curve cuts the x-
axis.

(3:2:1.2.1)

c. Find the radius of curvature of the curve
$$r^n = a^n \cos n\theta$$
. 07 (3:2:1.2.1)

Module-3

5. a. Obtain the Maclaurin's series expansion of
$$e^{\sin x}$$
 upto the term 06 (2:3:1.2.1) containing x^4 .

b. If
$$z = f(x+ct) + g(x-ct)$$
, prove that $\frac{\partial^2 z}{\partial t^2} = c^2 \frac{\partial^2 z}{\partial x^2}$.

c. If
$$u = \log \left(x^3 + y^3 + z^3 - 3xyz\right)$$
, then

prove that $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z} = \frac{3}{x + y + z}$.

6. a. If
$$u = f(x - y, y - z, z - x)$$
, show that $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z} = 0$

$$06 \quad (2:3:1.2.1)$$

b. If
$$u = x^2 + y^2 + z^2$$
, $v = xy + yz + zx$, $w = x + y + z$ then find $\frac{\partial(u, v, w)}{\partial(x, y, z)}$. **07** (3:3:1.2.1)

c. Examine the function
$$z(x, y) = x^4 + y^4 - 2(x - y)^2$$
 for extreme values. 07 (2:3:1.2.1)

Module-4

7. **a.** Solve:
$$6y^2 dx - x(x^3 + 2y) dy = 0$$
 06 (3 :4 : 1.2.1)

b. Solve:
$$ye^{xy}dx + (xe^{xy} + 2y)dy = 0$$
. **07** (3:4:1.2.1)

c. Find the orthogonal trajectories of the family
$$x^{2/3} + y^{2/3} = a^{2/3}$$
. 07 (1:4:1.2.1)

(OR)

8. a. A series circuit with resistance 'R' inductance 'L' and electromotive 06 (1:4:1.2.1) force 'E' is governed by the differential equation
$$L\frac{di}{dt} + Ri = E$$
 Where

R and L are constants and initially current i = 0. Find the current at any time't'.

b. Solve:
$$xy \left(\frac{dy}{dx}\right)^2 - (x^2 + y^2)\frac{dy}{dx} + xy = 0$$

$$(3:4:1.2.1)$$

c. Modify the following equation into Clairut's form. Hence obtain the or (2:4:1.2.1) associated general and singular solutions.
$$xp^2 + px - py + 1 - y = 0$$

Module-5

b. Change the order of the integration and hence evaluate
$$\int_{0}^{1} \int_{\sqrt{y}}^{2-y} xy \ dxdy$$
. (3 :5 : 1.2.1)

c. Write a Python Program to find
$$\int_{0}^{1} \int_{x}^{\sqrt{x}} \left(x^2 + y^2\right) dy dx$$
 07 (1:5:1.2.1)

Prove that:
$$\sqrt{1/2} = \sqrt{\pi}$$

b. Prove that
$$\beta(m,n) = \frac{\Gamma(m).\Gamma(n)}{\Gamma(m+n)}$$
. 07 (1:5:1.2.1)

c. Express the following integrals in terms of beta functions and hence 07 (1:5:1.2.1) evaluate
$$\int_{0}^{\infty} \frac{dx}{1+x^4}$$
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